

Deniable Encryption

and its applications

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What is "Deniability"?

Term referring to ability of rejecting accusations for some shady activities.

Political example:

- ▶ USA government allegedly planned an assassination of Cuba's leader
- ▶ Kennedy's administration: "we knew nothing about this!"
- ▶ no hard evidence found

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This is **plausible deniability**.

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- ▶ using cryptography and concealing keys can be highly suspicious
- ▶ ciphertext/signatures form perfect commitment
- ▶ long-lived keys
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Borisov, Goldberg, Brewer: Why not to use PGP in private communication.

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And what if key gets compromised?

Usually no security is guaranteed.

People are the weakest link the system security.

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Passwords and keys are likely to be disclosed:

- ▶ social engineering
- ▶ "black-bag" cryptoanalysis (trojans, key-loggers)
- ▶ extortion/coercion
- ▶ rubber-hose cryptoanalysis

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Concern not entirely unjustified:

- ▶ in certain countries public authorities can demand handing over encryption keys, e.g. *Regulation of Investigatory Powers Act* in UK

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Campaigners hit by decryption law

By Mark Ward

Technology correspondent, BBC News website

Animal rights activists are thought to be the first Britons to be asked to hand over to the police keys to data encrypted on their computers.

The request for the keys is being made under the controversial Regulation of Investigatory Powers Act (RIPA).



The police want to get at encrypted files

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- ▶ in certain countries public authorities can demand handing over encryption keys, e.g. *Regulation of Investigatory Powers Act* in UK
- ▶ political activists in non-democratic countries subject to rubber-hose cryptoanalysis

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Encrypting File Systems

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Implementations of *plausible deniability* but can we trust these programs?

B. Schneier says we should not!

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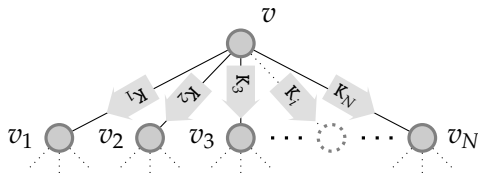
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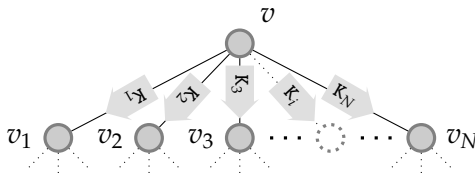
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- ▶ keep the data but throw out local copy of K
- ▶ key parts are erased after timeout – encrypted data is rendered useless afterwards

Deniable Encryption – a Decent Theoretical Approach

Alice is approached by the adversary that has previously intercepted a whole communication:

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But this is what **deniable encryption** is all about!

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We have a message M encrypted with algorithm E that uses a randomness r : $C = E(M, r)$.

How can we deliberately pick r' and construct $M' \neq M$ such that $E(M', r') = C = E(M, r)$?

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- ▶ allows virtually any opening, i.e. almost every M' matches a given ciphertext C
- ▶ M can be decided at the moment of the attack
- ▶ formally provable deniability property
- ▶ but not quite robust and rather impractical

Translucent Sets

t – some parameter

Translucent Set – an informal definition

Set $S \subset \{0, 1\}^t$ together with a trapdoor information d is said to be translucent iff

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When a random $x \in S$ is picked one can obtain a convincing proof that x is generated is this way!

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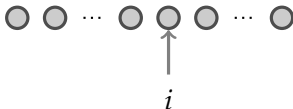


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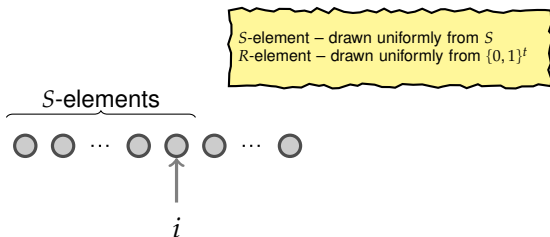


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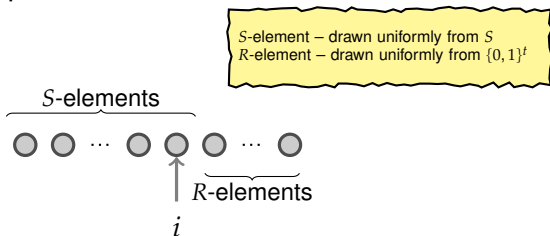


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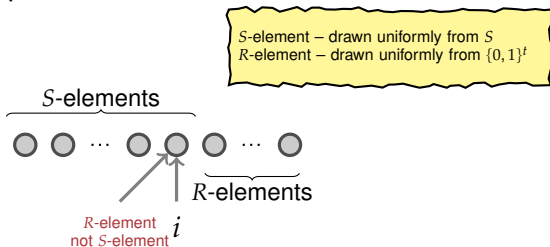


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- ▶ dishonest opening: it was $i - 1$ that was picked, not i
- ▶ lying not possible in case where $i = 0$

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Handing over a fake key will not do.

Can we offer Alice any form of cryptographical protection?

Secretly Embedded Extortion Warning

Give Alice a possibility of putting a special secret message in a signature indicating that signature is forced.

Such a warning is only readable by a fixed trusted party – *Savior of the Damned*.

The trusted can call the Police and send some help to Alice.

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- ▶ use the deniable encryption obviously
- ▶ transfer potential warnings transparently via subliminal channel

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Signatures issued by the adversary are perfectly acceptable for ordinary receivers (but not the trusted party)!

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What we have so far:

- ▶ K – a shared secret for Alice and the trusted party
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- ▶ R is quasi-random
- ▶ Alice computes the inner signature: $\sigma := \text{Sig}(M, R)$

A complete signature is (M, R, σ) .

Signature verification phase:

- ▶ ordinary verification – use verification of the inner signature $\text{Ver}(M, \sigma)$
- ▶ opening subliminal warning message – deciphering R using trapdoor d and comparing the result with $H(M \oplus K)$

Interesting applications of the deniable encryption:

- ▶ electronic voting protocol – protection against vote buying
- ▶ secure mutliparty computation